



Mathematics	Working towards expected outcomes	Working at expected outcomes	Working beyond expected outcomes
Autumn Term	<p>Your child is not yet making the expected progress within this course.</p> <p>Students working towards expected outcomes in Y13 can:</p> <ul style="list-style-type: none"> • Use and recall sine, cosine and tangent ratios; understand $\sec \theta$, $\operatorname{cosec} \theta$ and $\cot \theta$ as reciprocals and sketch their basic graphs. • Apply basic trig identity $\sin^2 \theta + \cos^2 \theta = 1$ to simplify simple expressions and solve straightforward equations. • Differentiate power functions x^n, $\sin x$ and e^x and in simple cases use the product, quotient and chain rules to find gradients at given points. • Plot simple parametric curves by substituting values of t; identify the corresponding (x, y) points. 	<p>Your child is achieving the expected progress for this point within the course.</p> <p>Students working at expected in Y13 can:</p> <ul style="list-style-type: none"> • Use addition and double-angle formulae $\sin(A+B)$, $\sin(A-B)$, $\cos(A+B)$, $\cos(A-B)$, $\tan(A+B)$, $\tan(A-B)$, $\cos 2A$ and $\sin 2A$ to solve trig equations in radians or degrees. • Express $a \cos \theta + b \sin \theta$ in the form $R \cos(\theta - \alpha)$ and solve for θ over specified intervals. • Understand domains, ranges and graphs of \arcsin, \arccos and \arctan. • Apply product, quotient and chain rules to differentiate combinations of polynomials, exponentials, logarithms and trig functions; find equations of tangents and normals. • Convert simple parametric forms to Cartesian equations (e.g. $x = 3 \cos t$, $y = 3 \sin t$) and sketch the resulting curves. 	<p>Your child is exceeding the expected progress.</p> <p>Students working beyond expected in Y13 can: In addition to the skills listed under ‘Working At’ for this topic, students working beyond expected outcomes can:</p> <ul style="list-style-type: none"> • Prove compound-angle and reciprocal-function identities (e.g. $\sec^2 \theta = 1 + \tan^2 \theta$) by geometric or algebraic methods. • Investigate how harmonic form is used in a Physics context • Derive key derivatives from first principles (e.g. $d/dx \sin x = \cos x$, $d/dx e^x = e^x$). • Solve complex problems involving parametric equations



Spring Term

- Perform implicit differentiation on simple relations like $x^2 + y^2 = 1$ to find dy/dx .

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Students working **towards** expected outcomes in Y13 can:

- Factorise quadratics and perform basic algebraic (polynomial) division; simplify simple algebraic fractions.
- Integrate x^n , $\sin kx$, $\cos kx$ and $e^{(kx)}$ by inspection, including constant of integration.
- Sketch quadratics, cubics, exponentials and reciprocal graphs; identify key features (intercepts, asymptotes).
- Locate roots of $f(x) = 0$ by sign-change on intervals; carry out simple fixed-point iteration.
- Add and scale 2D vectors in component form; calculate

- Solve related-rates problems linking dy/dx and dx/dt .

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Students working **at** expected in Y13 can:

- Decompose rational functions into partial fractions (distinct and repeated linear factors).
- Apply substitution and integration by parts to more complex integrals; use the trapezium rule for approximations.
- Solve first-order separable differential equations with given initial conditions.
- Work with modulus functions $y = |f(x)|$; sketch and solve related equations or inequalities.
- Perform Newton–Raphson iterations; sketch cobweb diagrams and discuss convergence.
- Extend vector methods to 3D (i, j, k); calculate distances, prove

Students working **beyond** expected in Y13 can:

- Factorise higher-degree polynomials (degree ≥ 3) using algebraic division and identify real roots; use the factor theorem systematically.
- Tackle complex integrals using a variety of methods with confidence
- Solve differential equations that need rearranging into separable form with partial fractions; interpret solutions graphically.
- Analyse and sketch modulus transformations with compound functions (e.g. $y = |f(g(x))|$)
- Use vector proofs to establish general results



magnitudes and draw vector diagrams.

- Expand $(1 + x)^n$ for small integer n

parallelism and solve simple plane/line problems.

- Expand $(1 + x)^n$ for rational n ; find the general term and use the series for approximations

